

Areeda-Turner in Two-Sided Markets*

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Abstract

We extend the Areeda-Turner rule to two-sided markets. We show that a two-sided monopolist may find it optimal to charge a price below marginal cost on one side of the market. Hence showing that the price is below marginal cost on one side of a two-sided market cannot be considered a sign of predation. We then argue for a two-sided Areeda-Turner rule that takes into account price-cost margins on both sides of the market. Two examples highlight that applying a one-sided Areeda-Turner rule may lead one to assess legitimate prices as predatory or to consider predatory prices as legitimate.

JEL Classification: L12, L41, L82.

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1 Introduction

In this paper, we extend the Areeda-Turner rule to two-sided markets. We do so by following the original logic of [Areeda and Turner \(1975\)](#). In their seminal article, the authors set out to identify a rational dividing line between legitimately competitive prices and prices that should be regarded as predatory. Adopting the classical definition of predation as the deliberate sacrifice of present revenues for the purpose of driving rivals out of the market and then recouping the losses, they proposed that “[u]nless at or above average cost, a price below reasonably anticipated (i) shortrun marginal costs or (ii) average variable costs should be deemed predatory, and the monopolist may not defend on the grounds that his price was "promotional" or merely met an equally low price of a competitor”. In addition “[r]ecognizing that marginal cost data are typically unavailable” they concluded that “[a] price below reasonably anticipated average variable cost should be conclusively presumed unlawful”.¹

Following the original logic of [Areeda and Turner \(1975\)](#), we seek a threshold for the price, such that a price below this threshold should be deemed predatory. We argue that such a threshold needs to take into account the specificity of two-sided markets. In these markets firms act as platforms and sell two different products or services to two distinct groups of customers.² An example is the newspapers’ market, in which publishers sell content to readers and advertising slots to advertisers. A two-sided market is further characterised by indirect network externalities between the two groups of consumers. These arise when the utility (or increase in profits) obtained by a customer (whether a final consumer or a firm) of one group depends on the number of customers of the other group and the two groups of customers do not internalise these externalities.³ In the case of newspapers, advertisers value advertising in a given newspaper more the more readers the newspaper has. Readers may or may not be affected by the amount of advertising in the newspaper⁴, but for the market to be two-sided already the presence of one indirect network effect is sufficient.⁵ Whereas customers do not internalize the externality (or externalities) above, two-sided platforms do internalize it (them) when deciding their optimal pricing

¹[Areeda and Turner \(1975\)](#), p. 733.

²See [Caillaud and Jullien \(2001, 2003\)](#), [Rochet and Tirole \(2002, 2006, 2003\)](#), [Evans \(2003\)](#), [Parker and van Alstyne \(2005\)](#) and [Armstrong \(2006\)](#).

³As a result, a two-sided platform is different from a firm selling complementary products. Indeed in the latter case there is only one group of customers who typically buy both goods (e.g. the ink-jet printer and the ink-jet cartridge) and thus, unless they are naive, they respond to changes in the prices of both. In a newspaper market, instead, a reader does not care about the price charged to advertisers and vice versa advertisers do not decide whether to place an ad in a newspaper based on the cover price of the latter.

⁴Empirical evidence so far seems to suggest that on average readers of daily newspapers are either indifferent to or slightly like advertising (which is usually not targeted but avoidable). See [Argentesi and Filistrucchi \(2007\)](#); [Fan \(2013\)](#) and [Filistrucchi et al. \(2012\)](#). Readers of magazines seem instead to positively value advertising (which is avoidable and more targeted). See [Kaiser and Wright \(2006\)](#) and [Kaiser and Song \(2009\)](#).

⁵See [Filistrucchi et al. \(2013\)](#).

strategies. As a result, the profit-maximizing prices by two-sided platforms may be very different from those charged by firms in one-sided markets.

As pointed out by [Rochet and Tirole \(2006\)](#), in a two-sided market, where two products or services are sold to two groups of customers, one can distinguish a price level and a price structure. The price level is the sum of the two prices, while the price structure is the ratio of the two prices. *When the unit of measurement of the goods or services sold on the two-sides are different and the matching of customers on the two sides is not one to one, the price level is not simply the sum of the two prices, but rather the sum of the two prices expressed in the same unit of measurement.* In the case of newspapers the price level is the sum of the cover price and the per-copy advertising revenues.⁶ Similarly, the price structure is the ratio of the two⁷. In two-sided markets not only the price level but also the price structure determines firms' profits. For instance, the profits of a publisher not only depend on how much revenues per copy of the newspaper it can raise but also on what percentage of revenues comes from readers versus advertisers: for a given revenue per copy, a business strategy that charges only readers may not be as profitable as one that charges only advertisers. Indeed, we observe free newspapers more often than we observe no-advertising newspapers.

The difference in pricing strategies that characterizes two-sided markets warrants in many instances a different antitrust treatment. A recent review discussing these issues is [Evans and Schmalensee \(2015\)](#).

[Parker and van Alstyne \(2005\)](#) were among the first to present an economic model highlighting that in two-sided markets pricing below marginal cost on one side may be a (nonstrategic) profit-maximising strategy. Indeed, by pricing below marginal cost on one side of the market a firm increases sales on that side, thus boosting demand and profits on the other side. [Wright \(2004\)](#) included the claim that “price below marginal cost on one side of the market is a sign of predation” among the eight fallacies which derive from applying a one-sided logic to two-sided markets.⁸

Despite the warnings of the economics literature, competition authorities and courts tend to analyse predatory claims with a one-sided logic. In the recent case [Bottin Cartographes vs Google](#)⁹, for instance,

⁶One can also express the price level in terms of advertising pages. In that case it is the sum of the advertising price and the circulation revenues per-advertising-page.

⁷Note that such a ratio is equivalent to the ratio between the revenues from the two sides. In the newspapers' business the ratio of circulation revenues to advertising revenues (or vice versa) is sometimes called the “financing mix”.

⁸To our knowledge, no paper discusses conditions for predation on prices to take place in a two-sided market. A partial exception is [Motta and Vasconcelos \(2012\)](#) that presents a model of platform competition in which below-cost pricing can be used to deter entry of a more efficient rival. However, the result in [Motta and Vasconcelos \(2012\)](#) crucially depends on the fact that one of the two firms is already present in the market, while the other is trying to enter.

⁹[Bottin Cartographes v. Google Inc. and Google France Srl](#), Commercial Court of Paris, 15th chamber, 31 January 2012, available at http://www.legalis.net/spip.php?page=jurisprudence-decision&id_article=3327. In July 2009 Bottin Cartographes SAS (hereafter “Bottin”) filed a lawsuit before the Commercial Court of Paris (Paris Tribunal de Commerce) against Google Inc. and Google France Srl (hereinafter collectively “Google”) for alleged abuse of dominant position in the market of online mapping services allowing stores geolocation on firms' websites. Bottin is a multimedia mapping company providing, among

the Commercial Court of Paris found Google guilty of abuse of dominant position in the market for online maps allowing stores geolocation.¹⁰ The Court reached its decision by simply considering that the price of Google Maps API, being equal to 0 €, was necessarily lower than the production costs of the service. Interestingly, the Court stopped just short of recognizing the implications for competition policy of the two-sided business strategy of Google, as it recognized that Google, according to the contracts, would be able to insert advertising in its Google Maps API service and therefore sell targeted advertising.

Judgements like the one above may partly be due to the fact that most policy contributions so far, such as [Wright \(2004\)](#), have criticized the application of the one-sided Areeda-Turner rule to two-sided markets without suggesting an alternative. Even those policy contributions, such as [Fletcher \(2007\)](#) or [Evans and Noel \(2008\)](#), that recognized the necessity to provide guidance to practitioners fall short of providing new applicable methods. In fact, when Google appealed the decision of the Commercial Court of Paris, the Court of Appeal of Paris¹¹ decided to suspend the proceeding and ask the French Competition Authority to deliver an opinion on whether Google's conduct had to be considered anticompetitive.¹² The request of the Court of Appeal highlights the uncertainty among practitioners regarding criteria to establish predatory pricing in two-sided markets.

We contribute to filling this gap by explaining how one should modify the Areeda-Turner rule to account for the two-sidedness of a market. Testing for predatory pricing in a two-sided market must take into account the presence of the indirect network effects between the two sides. Hence, it has to recognize that price-cost margins on the two sides of the market are interrelated. We thus show that one needs to compare the overall price level with the joint marginal cost of the two-sides of the market. Since, as already noted by [Areeda and Turner \(1975\)](#), marginal cost data are difficult to obtain, one should compare the overall price level with the overall average variable cost.

[Filistrucchi et al. \(2013\)](#) point out that there exist two-types of two-sided markets. Two-sided non-transaction markets are characterized by the absence of a transaction between the two sides of the market

others, online map applications allowing users to locate addresses and create itineraries online, which compete in France with the equivalent service Google Maps API (Application Programming Interface) provided by Google. While Bottin offers its service in exchange of an annual fee and an ex post compensation based on actual consumption, the ordinary version of Google Maps API is provided to the customers on a free basis. Bottin claimed that this had to be considered a predatory pricing and that by doing so Google aimed at extending its dominant position on the market of online search to the connected relevant market.

¹⁰More precisely, with its decision of 31 January 2012 the Commercial Court of Paris found Google guilty of abuse of dominant position pursuant to Article L-420-2 paragraph 1 of the French Commercial Code and, as a consequence, awarded Bottin 500,000 € damages and interests, in addition to ordering Google to publish the judgment at its expense in several French and international newspapers.

¹¹*Bottin Cartographes v. Google France and Google Inc.* Court of Appeal of Paris, 5th Pole, 5th Chamber, 20 November 2013, available on http://www.legalis.net/spip.php?page=jurisprudence-decision&id_article=3942

¹²The opinion of the Competition Authority has not been made public yet. In fact, it can be disclosed only after the ruling of the Appeal Court (art. L.462-3 of the French Code of Commerce), which has not been handed out yet.

and, even though an interaction is present, it is usually not observable, so that a per-transaction (or per-interaction) fee or a two-part tariff is not possible. Typical examples are media markets. Two-sided transaction markets are instead characterized by the presence and observability of a transaction between the two groups of platform users. As a result, the platform is able to charge not only a price for joining the platform, but also one for using it, i.e. it can ask a two-part tariff. Examples in this category include payment cards schemes, virtual marketplaces, auction houses and operating systems.

The extension of the Areeda-Turner rule that we develop is in line with the suggestion by [Evans \(2003\)](#) for transaction markets.¹³ This suggestion was however not derived from a formal model. In addition, [Evans \(2003\)](#) recognized the difficulty to provide guidance on how to implement the test in two-sided non-transaction markets. Our formulas, which are derived from the application of the same logic as [Areeda and Turner \(1975\)](#), are applicable instead to two-sided non-transaction markets, such as the market for newspapers we consider in Section 3. However, following the same approach also for two-sided transaction markets, one would indeed obtain similar formulas to those proposed by [Evans \(2003\)](#).

Discussing predatory pricing in two-sided transaction markets, [Fletcher \(2007\)](#) suggested to draw a predatory pricing rule from the finding in [Rochet and Tirole \(2006\)](#) that the markup on each side of a two-sided market can be calculated as in a one-sided market, with the caveat that from the marginal cost one needs to subtract any extra revenue that the extra sales on that side of the market generate on the other side of the market. It turns out that the latter intuition is, to some extent, true also for two-sided non-transaction markets. By deriving our conditions from a formal model, we explain what this extra term is in a two-sided non-transaction market and highlight that one also needs to take into account the extra cost incurred on the other side of the market.

We then apply our two-sided Areeda-Turner rule to two cases in the newspaper industry. We first look at the price war in the UK quality daily newspapers in the '90s and test whether the pricing strategy of The Times from September 1993 to December 1995 was an example of predatory pricing, as claimed by its competitors, particularly by the Independent. The case was investigated by the Office of Fair Trading (OFT) that concluded against the existence of predatory behaviour. It enjoyed considerable publicity at the time for its political implications and has not ceased to be debated, not only because the OFT decision, whether right or wrong, did not include much empirical investigation but also because, looking at it today in light of the theory of two-sided markets, it is striking that the OFT did not carry out any analysis of the advertising market. We show that, had it done so, it would have found that the pricing

¹³[Evans \(2003\)](#) calls them “matchmaking” two-sided markets.

strategy of the Times was probably not predatory, even taking for granted the cost estimates of The Independent, according to which the Times was sold to readers at a price below average variable cost. We then discuss the case of Aberdeen Journals, whose pricing strategies between 1996 and 2000 were also investigated by the OFT. It was a case of alleged predation involving free newspapers in Scotland. The OFT and the Competition Appeal Tribunal (CAT) calculated price-cost margins and concluded that advertising prices set by Aberdeen journals in response to the entry of Aberdeen & District Independent were below average variable costs and, therefore, predatory. We argue that, although readers did not pay for the newspapers, the OFT took the right approach in taking into account also the costs incurred on the readers side.

The paper is organised as follows: Section 2 compares monopoly pricing in two-sided markets to monopoly pricing in one-sided markets and extends the one-sided Areeda-Turner rule to two-sided markets. In Section 3 we analyse the two cases of alleged predatory behaviour in the market for daily newspapers, namely the Times vs. Independent war and the Aberdeen Journals case. Section 4 concludes.

2 Areeda-Turner from one to two sides

2.1 One-sided versus two-sided monopoly pricing

We here show the difference between monopoly pricing in one-sided and two-sided markets.

Our starting point is the well-known formula for the mark-up in a one-sided monopoly

$$\frac{(P - \frac{\partial C}{\partial Q})}{P} = \frac{1}{|\eta_P^Q|} \quad (1)$$

where $C(\cdot)$ is the monopolist cost function and η_P^Q is the elasticity of market demand Q with respect to the price P .

This formula reminds us that a short-run profit-maximizing monopolist in a one-sided market will set a price above marginal cost.

A monopolist in a two-sided market sets P^A on side A of the market and P^R on side R of the market¹⁴ so as to maximize profits

¹⁴Our empirical examples below are for the daily newspaper market. Hence, we denote the two sides of the market with A (for advertisers) and R (for readers).

$$\pi = P^A Q^A + P^R Q^R - C(Q^A, Q^R) \quad (2)$$

subject to the constraints

$$\begin{aligned} Q^R &= Q^R(P^R, Q^A) \\ Q^A &= Q^A(P^A, Q^R) \end{aligned} \quad (3)$$

where the demands $Q^R(\cdot)$ and $Q^A(\cdot)$ are functions of prices on the same market side and of quantities on the other side of the market.

In two-sided markets, quantities on one market side are functions of prices on that market side and quantities on the other market side. In the context of the newspaper industry, this means that the amount of advertising demanded is a function of the advertising price and the number of readers, while the number of readers is a function of the cover price and the quantity of advertising.

[Filistrucchi and Klein \(2013\)](#) show that if

$$\left| \frac{\partial Q^A}{\partial Q^R} \frac{\partial Q^R}{\partial Q^A} \right| < 1 \vee P^A, P^R \quad (4)$$

i.e. if the product of the indirect network effects is not too large¹⁵, the consumers' coordination game, identified by [Armstrong \(2006\)](#) and further discussed by [Weyl \(2010\)](#), has a unique solution and the set of constraints can be rewritten as

$$\begin{aligned} Q^R &= \hat{Q}^R(P^R, P^A) \\ Q^A &= \hat{Q}^A(P^A, P^R) \end{aligned} \quad (5)$$

where the demands $\hat{Q}^R(\cdot)$ and $\hat{Q}^A(\cdot)$ are now functions of prices on both market sides only.

In other words, if the condition above holds, although customers do not internalize the link between demands, there exist reduced form demands which depend on prices on the two sides of the market. In the context of the newspaper market, it implies that it is possible to express both advertising demand and readership demands as functions of the advertising price and the newspaper price.¹⁶ Intuitively, this means that, given a set of prices chosen by the platform, there is only one set of quantities: the

¹⁵In the newspaper example, consider the case of one more reader buying the (monopolist) newspaper. This starts a loop: more readers, more advertising, fewer readers, less advertising, more readers... and so on. Intuitively the condition above ensures that this loop converges for any set of prices. If so, when the publisher changes one price, the resulting change in quantities is finite.

¹⁶This result is used in [Affeldt et al. \(2013\)](#) to derive formulas for Upward Pricing Pressure in a two-sided market. An equivalent condition for two-sided markets is assumed to hold in [Kaiser and Wright \(2006\)](#) who bring the Hotelling model of [Armstrong \(2006\)](#) to the data.

consumers coordination game, due to the fact that optimal decisions of customers on side A depend on decisions of customers on side R and vice versa, has a unique equilibrium.

Substituting these into the profit function above, one obtains

$$\pi = P^A \hat{Q}^A(P^A, P^R) + P^R \hat{Q}^R(P^R, P^A) - C(\hat{Q}^A(P^A, P^R), \hat{Q}^R(P^R, P^A)) \quad (6)$$

Then, the monopolist's profit maximizing prices solve the first order conditions

$$\hat{Q}^A + \left(P^A - \frac{\partial C^A}{\partial \hat{Q}^A} \right) \frac{\partial \hat{Q}^A}{\partial P^A} + \left(P^R - \frac{\partial C^R}{\partial \hat{Q}^R} \right) \frac{\partial \hat{Q}^R}{\partial P^A} = 0, \quad (7)$$

$$\hat{Q}^R + \left(P^A - \frac{\partial C^A}{\partial \hat{Q}^A} \right) \frac{\partial \hat{Q}^A}{\partial P^R} + \left(P^R - \frac{\partial C^R}{\partial \hat{Q}^R} \right) \frac{\partial \hat{Q}^R}{\partial P^R} = 0 \quad (8)$$

Filistrucchi and Klein (2013) show that one can obtain the derivatives of the reduced form demands from the derivatives of the original demands using the implicit function theorem¹⁷ :

$$\begin{pmatrix} \frac{\partial \hat{Q}^A}{\partial P^A} & \frac{\partial \hat{Q}^A}{\partial P^R} \\ \frac{\partial \hat{Q}^R}{\partial P^A} & \frac{\partial \hat{Q}^R}{\partial P^R} \end{pmatrix} = \frac{1}{d} \begin{pmatrix} \frac{\partial Q^A}{\partial P^A} & \frac{\partial Q^A}{\partial Q^R} \frac{\partial Q^R}{\partial P^R} \\ \frac{\partial Q^R}{\partial Q^A} \frac{\partial Q^A}{\partial P^A} & \frac{\partial Q^R}{\partial P^R} \end{pmatrix} \quad (9)$$

where $d = 1 - \frac{\partial Q^A}{\partial Q^R} \frac{\partial Q^R}{\partial Q^A} > 0$. Note that the sign of the cross-price derivatives depends on the sign of the network effects: if the network effect is positive the cross-price derivative is negative, if the network effect is negative the cross-price derivative is positive.

From the first order conditions in (2) and (3), one can obtain the monopolist's markup on each side of the market

$$\left(\frac{P^A - \frac{\partial C}{\partial \hat{Q}^A}}{P^A} \right) = \frac{1}{|\eta_{P^A}^{\hat{Q}^A}|} + \left(\frac{P^R - \frac{\partial C}{\partial \hat{Q}^R}}{P^R} \right) \frac{R^R}{R^A} \frac{\eta_{P^A}^{\hat{Q}^R}}{|\eta_{P^A}^{\hat{Q}^A}|} \quad (10)$$

$$\left(\frac{P^R - \frac{\partial C}{\partial \hat{Q}^R}}{P^R} \right) = \frac{1}{|\eta_{P^R}^{\hat{Q}^R}|} + \left(\frac{P^A - \frac{\partial C}{\partial \hat{Q}^A}}{P^A} \right) \frac{R^A}{R^R} \frac{\eta_{P^R}^{\hat{Q}^A}}{|\eta_{P^R}^{\hat{Q}^R}|} \quad (11)$$

where R^R are revenues from readers, R^A are revenues from advertisers, $\eta_{P^A}^{\hat{Q}^A}$ is the total own-price elasticity on the advertisers' side, $\eta_{P^R}^{\hat{Q}^R}$ is the total own-price elasticity on the readers' side, while $\eta_{P^R}^{\hat{Q}^A}$ and $\eta_{P^A}^{\hat{Q}^R}$ are the total cross-price elasticities.

¹⁷This is done also in Affeldt et al. (2013) to estimate the diversion ratios necessary to apply Upward Pricing Pressure in a two-sided market.

To understand these total elasticities, note that the total elasticity $\eta_{P^R}^{\hat{Q}^R}$ includes, in addition to the changes in Q^R directly due to the change in P^R , also the additional changes in Q^R due to the indirect network effects. Consider the newspaper example. Suppose the monopolist increases the price to the readers P^R while keeping the price to the advertisers P^A unchanged; as a result the quantity of readers Q^R decreases: this effect would be captured by a direct (or partial) elasticity $\eta_{P^R}^{Q^R}$. However, the decrease in the number of readers Q^R also decreases the quantity of advertising sold Q^A (as advertisers willingness to pay for an advertising slot in a newspaper increases with the number of readers). In turn, the decrease in advertising sold Q^A increases the quantity of readers Q^R (if readers of newspapers are annoyed by advertising), and so on. A similar reasoning applies to the total elasticities $\eta_{P^R}^{\hat{Q}^A}$, $\eta_{P^A}^{\hat{Q}^R}$ and $\eta_{P^A}^{\hat{Q}^A}$, which measure the effects of an increase in P^R on Q^A and of P^A on Q^R and on Q^A .

From (9) one can check that the total own-price elasticities, $\eta_{P^R}^{\hat{Q}^R}$ and $\eta_{P^A}^{\hat{Q}^A}$, are negative when the condition for the existence of the reduced form demand functions is satisfied (i.e. when $\left| \frac{\partial Q^A}{\partial Q^R} \frac{\partial Q^R}{\partial Q^A} \right| < 1$). As a result, the first term on the right hand side, in both equation (10) and equation (11), is positive. In both cases it resembles the term on the right hand side in the equation (1), but differs in that the elasticities in equations (10) and (11) include the indirect network effects.

The existence of a second term on the right hand side, in both equation (10) and equation (11), is also due to the presence of the indirect network effects. Its sign depends on the sign of total cross-price elasticities with respect to the readers' price and the advertisers' price ($\eta_{P^R}^{\hat{Q}^A}$ and $\eta_{P^A}^{\hat{Q}^R}$ respectively) and on the sign of the markup on the other side of the market (either $\left(\frac{P^R - \frac{\partial C}{\partial Q^R}}{P^R} \right)$ or $\left(\frac{P^A - \frac{\partial C}{\partial Q^A}}{P^A} \right)$). Hence, the markups on the two-sides of the market are interrelated.

Turning to total cross-price elasticities $\eta_{P^R}^{\hat{Q}^A}$ and $\eta_{P^A}^{\hat{Q}^R}$, they can be positive or negative, depending on the sign of the total derivatives $\frac{\partial \hat{Q}^A}{\partial P^R}$ and $\frac{\partial \hat{Q}^R}{\partial P^A}$ respectively, which in turn depend on the signs of the indirect network effects $\frac{\partial Q^A}{\partial Q^R}$ and $\frac{\partial Q^R}{\partial Q^A}$, as shown in equation (9).

Without loss of generality, let us consider the markup on side R given by equation (11). Substituting (10) into (11), one obtains

$$\left(\frac{P^R - \frac{\partial C}{\partial Q^R}}{P^R} \right) = \frac{\left| \eta_{P^A}^{\hat{Q}^A} \right| + \frac{R^A}{R^R} \eta_{P^R}^{\hat{Q}^A}}{\left| \eta_{P^A}^{\hat{Q}^A} \right| \left| \eta_{P^R}^{\hat{Q}^R} \right| - \eta_{P^A}^{\hat{Q}^R} \eta_{P^R}^{\hat{Q}^A}} \quad (12)$$

where $\left| \eta_{P^A}^{\hat{Q}^A} \right| \left| \eta_{P^R}^{\hat{Q}^R} \right| - \eta_{P^A}^{\hat{Q}^R} \eta_{P^R}^{\hat{Q}^A} > 0$ because of assumption (4).

Assume $\eta_{P^R}^{\hat{Q}^A} < 0$. This implies that customers on side A attach a positive value to customers on side

R.¹⁸ Then the mark-up on side R is negative if

$$\left| \eta_{P^A}^{\hat{Q}^A} \right| < \frac{R^A}{R^R} \left| \eta_{P^R}^{\hat{Q}^A} \right| \quad (13)$$

i.e. if the total elasticity of \hat{Q}^A with respect to P^R is (sufficiently) larger than the total elasticity of \hat{Q}^A with respect to P^A and revenues from side A are more important than revenues from side R. In this case, it is more profitable to lower the price to customers on side R and increase the price to customers on side A.

We have thus shown that, depending on the sign and size of the own-price effects and the indirect network effects, *it may be a short-run profit maximizing strategy for a monopolist in a two-sided market to set a price below marginal cost on one side of the market.* In the context of our newspaper example, it may be the case that a monopolist publisher finds it privately optimal to distribute its newspaper for free to readers while selling advertising slots to advertisers.

2.2 A two-sided Areeda-Turner rule

Given that a monopolist might find it profit maximizing in the short-run to set a price below marginal cost on one side of a two-sided market, setting a price below marginal cost on one side only cannot be considered a sign of predation. Hence, as claimed also by [Evans \(2003\)](#) and [Wright \(2004\)](#), the Areeda-Turner rule cannot be applied to only one side of a two-sided market. One needs instead to apply the logic of [Areeda and Turner \(1975\)](#) to two-sided markets.

Clearly a possibility for a two-sided Areeda-Turner rule would be to require the price to be below marginal cost on each side of the market for the pricing strategy of a dominant firm to be presumed predatory. However, this would restrict the set of prices found to be predatory more than the Areeda-Turner rule does in one-sided markets.

In such markets, the benchmark is a price equal to marginal cost. Any lower price implies that the monopolist is making a loss at the margin, while a profit-maximizing monopolist will make a gain at the margin. In addition, if marginal costs are constant, any price lower than marginal cost also implies that the monopolist is making negative variable profits.

The benchmark should be the same in two-sided markets: prices such that the monopolist is making an overall loss at the margin should be considered predatory. For such prices it should also be the case that, if marginal costs are constant, a monopolist makes negative profits. Instead, choosing price below

¹⁸This too is without loss of generality, because in a two-sided market customers of at least one side must attach a positive value to customers of the other side.

marginal cost on each side of a two-sided market, would consider non-predatory a substantial set of prices at which a monopolist is making a loss at the margin: all those prices for which the monopolist makes a marginal gain on one side and a marginal loss on the other side but the latter does not compensate for the former.

To see this, consider the case in which the monopolist is making a loss on side R, i.e. $P^R - \frac{\partial C}{\partial \hat{Q}^R} < 0$. Then, for the monopolist to make a loss overall, it is not necessary that it also makes a loss at the margin on side A, i.e. it is not necessary that $P^A - \frac{\partial C}{\partial \hat{Q}^A} < 0$. Instead it is necessary that the marginal gain on side A is not enough to offset the marginal loss on side R. Similarly for the side A.

Instead, according to an Areeda-Turner rule for two-sided markets, prices on side R should be considered predatory if

$$\left(P^R - \frac{\partial C}{\partial \hat{Q}^R} \right) + \left(P^A - \frac{\partial C}{\partial \hat{Q}^A} \right) \frac{\partial Q^A}{\partial Q^R} < 0 \quad (14)$$

while prices on side A should be considered predatory if

$$\left(P^A - \frac{\partial C^A}{\partial \hat{Q}^A} \right) + \left(P^R - \frac{\partial C^R}{\partial \hat{Q}^R} \right) \frac{\partial Q^R}{\partial Q^A} < 0 \quad (15)$$

In other words, for a two-sided market one can reformulate the Areeda-Turner rule as follows:

When the sum of the prices on the two-sided market, weighted by the marginal network effect, is lower than the sum of the corresponding marginal costs, weighted by the network effect, prices should be judged predatory.

Conditions(14) and (15) imply not only that the profit margin on one side should be negative but also that the weighted sum of the profit margins on the two-sides should be negative, when the appropriate network effect is taken as the weight. Hence, a finding of negative profit margins on both sides would be sufficient to justify a presumption of predatory pricing in the Areeda-Turner spirit, but it would not be necessary.

In fact, whereas there is no guarantee that the profit margin on one side is positive, even for a profit maximizing monopolist, from the first order conditions (7) and (8), using (9) to substitute for the derivatives, one obtains

$$\left(P^R - \frac{\partial C^R}{\partial \hat{Q}^R} \right) + \left(P^A - \frac{\partial C^A}{\partial \hat{Q}^A} \right) \frac{\partial Q^A}{\partial Q^R} = - \frac{\hat{Q}^R}{\partial \hat{Q}^R / \partial P^R} > 0 \quad (16)$$

$$\left(P^A - \frac{\partial C^A}{\partial \hat{Q}^A}\right) + \left(P^R - \frac{\partial C^R}{\partial \hat{Q}^R}\right) \frac{\partial Q^R}{\partial Q^A} = -\frac{\hat{Q}^A}{\partial \hat{Q}^A / \partial P^A} > 0 \quad (17)$$

These conditions show that for a profit-maximizing monopolist the weighted sum of the profit margins in (14) and (15) would be positive. As argued above, for such a monopolist on at least one side of the market the profit margin should be positive, but on one side it could be negative. Conditions (15) and (14) also ensure that predatory prices are such that variable profits are negative if average variable costs are constant.

Finally, recognizing not only, as Areeda and Turner (1975), that marginal cost data are typically unavailable, but also that estimates of the marginal network effect are not easy to obtain, prices should be presumed predatory if

$$(P^R - AVC^R) + \frac{Q^A}{Q^R} (P^A - AVC^A) < 0 \quad (18)$$

or, equivalently¹⁹, if

$$(P^A - AVC^A) + \frac{Q^R}{Q^A} (P^R - AVC^R) < 0 \quad (19)$$

Note that these conditions preserve the properties that: a) the left-hand side is positive for a profit maximizing monopolist b) if a set of prices satisfy it and marginal costs are constant, variable profits are negative. These same properties are preserved in a one-sided market when one uses $(P - AVC) < 0$ instead of $(P - \frac{\partial Q}{\partial C}) < 0$.

To conclude, for most practical purposes, for a two-sided market one can reformulate the Areeda-Turner rule as follows:

A price level below the reasonably anticipated average variable cost level should be judged predatory.

3 An application to Daily Newspapers

To illustrate the results derived in the previous section, we now analyse two alleged cases of predatory pricing in the newspaper industry, a typical two-sided industry. The first case, the Times-Independent

¹⁹Only in the special case in which one side does not affect the other, e.g. when readers do not care about the number of ads in the newspaper, condition (19) will become

$$(P^A - AVC^A) < 0$$

while condition (18) will remain unchanged. In this case, the two practical conditions would not be equivalent.

price war, highlights the importance of using the correct Areeda-Turner rule for two-sided markets rather than the one-sided rule and concerns the quality newspaper market, where both readers and advertisers pay to access the platform. The second, the Aberdeen Journals case, concerns the market for free newspapers and illustrates how one should deal with predatory allegations in those two-sided markets in which one side of the market does not pay. In fact, that customers on one side may not pay is a common feature of many two-sided markets, from the traditional free-to-air TV market to many recent online services (such as Internet search, online news, free email accounts and social networks).

3.1 The Times - Independent price war

During the early 1990s the UK market for quality broadsheet newspapers had experienced stable cover prices. On the 1st September 1993, The Times, The Independent and The Guardian were priced at 45p and the Daily Telegraph at 48p.

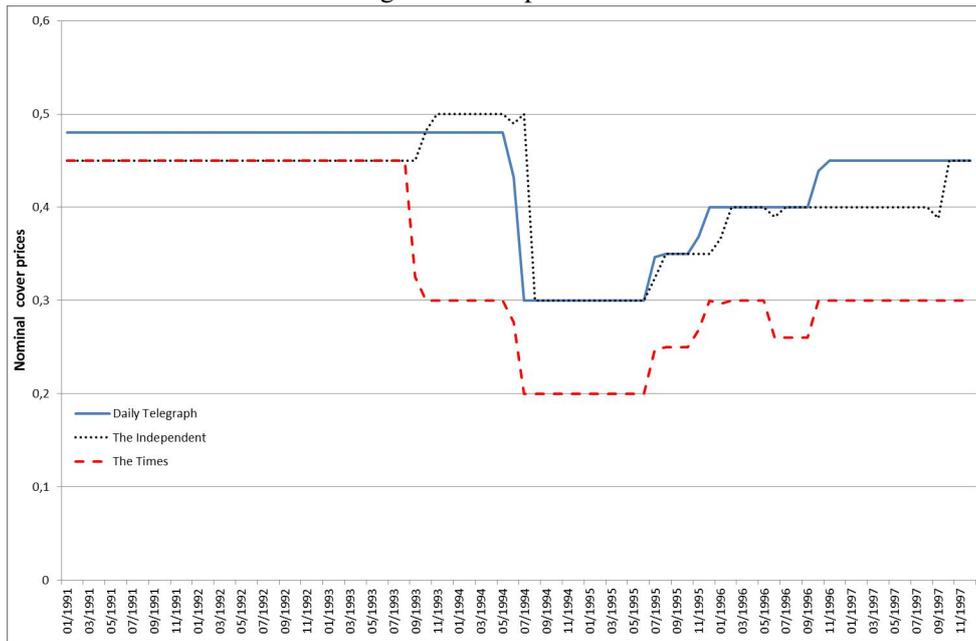
On 6 September 1993 The Times lowered its price by 33%, from 45p to 30p. As its circulation revenues came under pressure, on 12 October 1993 The Independent raised its price from 45p to 50p. On 23 June 1994, while the Daily Telegraph matched the new price of The Times lowering its price by 37.5%, the Independent was offered on a one-day sale for 20p, with the following announcement appearing on its first page: “We remain dedicated to journalism of the highest quality and integrity. Readers will understand that this can never be cheap”. On 24 June 1994 The Times lowered its price by another 33%, from 30p to 20p, bringing the overall price cut to 55%. Finally, on 1 August 1994 The Independent was also forced to lower its price by 40%, from 50p to 30p. Figure 1 depicts this price war graphically.²⁰

The Independent claimed to be the target of a predatory attempt by the Times. It held that the prices of 30p and 20p per copy of The Times amounted respectively to a “£18m a year” and a “£30m a year” subsidy. It filed a complaint to the OFT. A “deep pocket” predator story was put forward, according to which NIN who owned the Times could afford to sustain higher losses than the Independent, thanks to cross-subsidization from other profitable media businesses it owned.

The OFT investigations into the price cuts of September 1993 and June 2004 led to the conclusion that The Times was not dominant in the readers’ market for national daily newspapers and that The Independent was just one of its competitors. Hence The Times could not reasonably expect that the losses it would incur in the predatory campaign would be recouped by a higher price after The Independent

²⁰Note that the graph reports average prices per month. Hence, unless the price change takes place on the first day of the month, the changes appear in the graph a bit smoother than one would expect given the description in the text.

Figure 1: The price war



would have exited the market. As a result the OFT dismissed the claims of predation.

The price war influenced the public discussion on the adoption of the new competition act in 1998: the House of Lords sought, without success, to introduce an amendment to the bill that would specifically prohibit predatory prices, even in the absence of a dominant position by the predator, in circumstances which might reduce the diversity of the press.

As also shown in Figure 1, from July 1995 cover prices of The Times, the Daily telegraph and The Independent started to rise and from January 1996 they stabilized again.

However in 1998, following another formal complaint by The Daily Telegraph, The Guardian and The Independent, the OFT investigated The Times’ behavior during the period between June 1996 and January 1998 when the Monday edition was sold for 10p, and concluded that such prices were predatory.²¹

Interestingly, in all its investigations, the OFT failed to recognize the two-sidedness of the market and the fact that the losses from the readers’ market might be covered by gains on the advertising market.

We draw on the data in [Behringer and Filistrucchi \(2011\)](#) to show that despite the huge cut in prices, the pricing strategy of The Times in 1993 and 1994 could not be presumed predatory according the Areeda-Turner rule properly modified to take into account two-sidedness of the market, i.e. according to equation (18). [Behringer and Filistrucchi \(2011\)](#) argue that the observed price war can be rationalized

²¹ Since, this behavior had ended 16 months before the end of the investigation, the OFT decided not to refer News International (publisher of The Times) to the Competition Commission for charges and accepted assurances given by the publisher that it would notify and provide detailed justification for any future reductions of its cover price.

by the boom in the advertising market, which shifted the optimal business model of publishers towards more advertising financing.

In particular, on the readers' side of the market, we use monthly observations of circulation and cover prices. On the advertising side of the market we use monthly observations on advertising quantity and revenues of The Times.²² We recover advertising prices dividing revenues by quantity. Our sample covers the period 1991-1997.

According to The Independent the average variable cost of the Times was 32.5p (17.5p went to the distribution and the cost of printing a copy was 15p). Since this was reported by the complainant, if anything the estimate should be biased upward and the resulting price-cost margins should be biased towards predation. We thus use this estimate (adjusting it by the monthly CPI) to estimate the overall markups of the Times from 1991 to 1997 per copy sold, taking into account both the cover price and the revenues from advertising as suggested by the two-sided Areeda-Tuner rule in (18).²³ Figure 2 shows that, although the overall per copy markup of The Times dropped substantially during the price war, it always remained above zero. Clearly, with a marginal cost of 32.5p at a price of 30p or 20p, the price-cost margin on the readers' side was instead negative. Applying the Areeda-Turner rule to the readers' side of the market only would lead to the conclusion that prices are predatory.

However, as shown by Figure 3, the cut in prices led to a substantial increase in circulation. Figure 4 shows that the higher circulation led to an increase in advertising revenues. The latter effect is taken into account by a two-sided Areeda-Turner rule, but not by a one-sided Areeda-Turner rule. This explains why they lead to different conclusions.

3.2 The Aberdeen journals' case

While the case *The Times vs. Independent* concerned alleged predation on the cover price in the market for national newspapers, the case of *Aberdeen Journals* concerned a case of alleged predation on the advertising price in the market for local newspapers. More importantly, the case of *Aberdeen journals* concerned a two-sided market where one side did not pay, but, differently from the recent *Bottin Cartographes vs Google* case we discussed in the introduction, the allegations of predation referred to pricing on the paying side. This raises additional issues with regard to the application of the correct two-sided Areeda-Turner rule.

²²Data on circulation come from those collected by the Audit Bureau of Circulation (ABC). Data on prices were collected from newspaper publishers themselves. These data were acquired from Nielsen Media Research UK.

²³Note that we consider all advertising costs to be fixed in the short-run. This assumption is in line with the outcome of the discussion, by market participants and the OFT, of newspaper costs in the case *Aberdeen Journals*. The rationale is that advertising staff is fixed in the short-run and printing one page of content or one page of advertising has the same cost.

Figure 2: Two-sided and one-sided price-cost margins for The Times

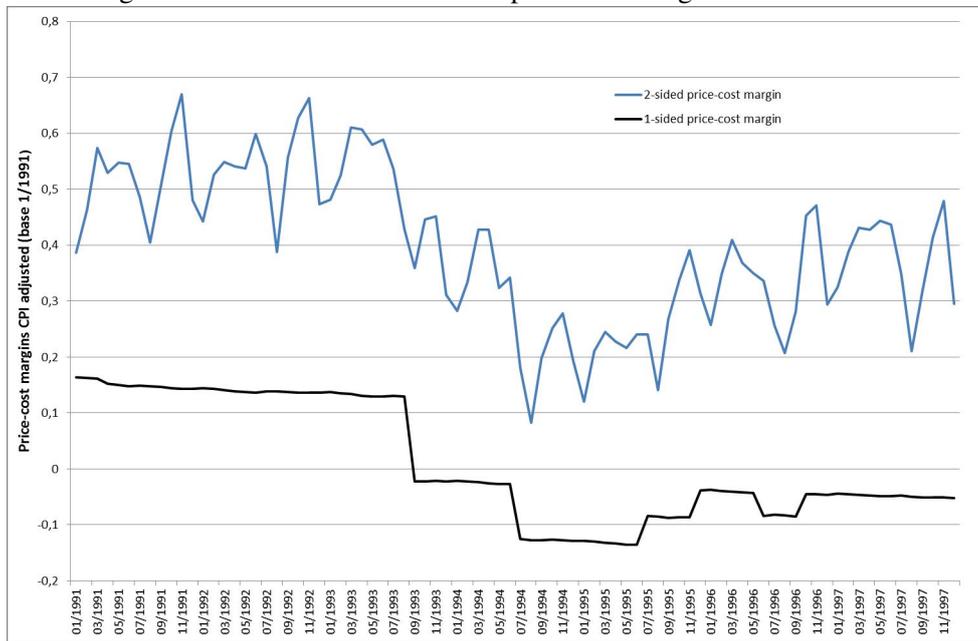
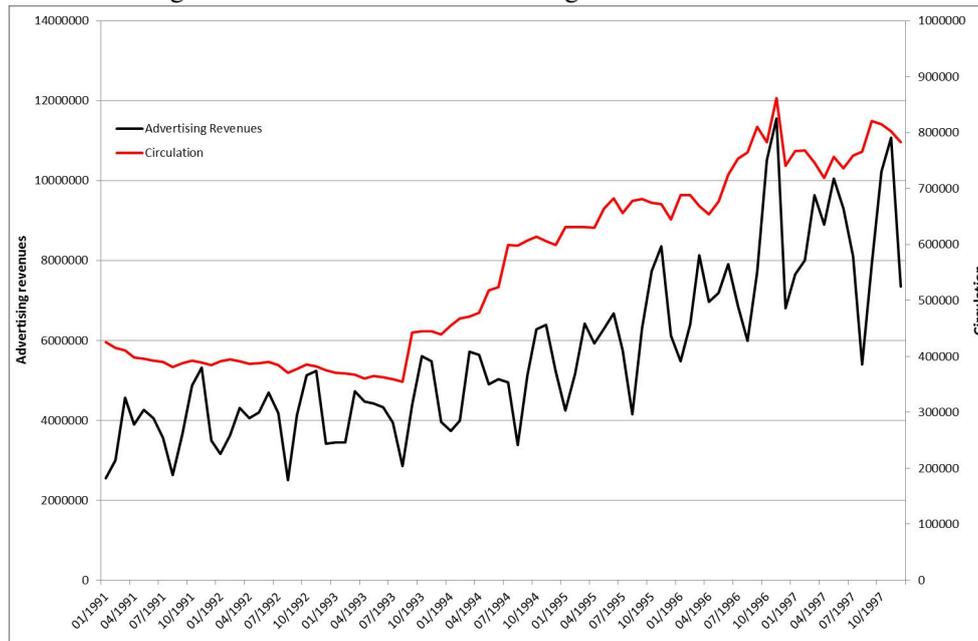


Figure 3: Cover price and circulation of The Times



Figure 4: Circulation and advertising revenues of The Times



The case just follows in time the Times-Independent price war discussed in the previous section. After the introduction of the UK Competition Act on 1 March 2000, which made the abuse of a dominant position illegal, *Aberdeen & District Independent* complained that Aberdeen Journals Limited was engaging in predatory pricing of advertising space in its free newspaper Herald & Post. On 16 July 2001, and again on 29 September 2002²⁴, the OFT issued its decision against Aberdeen Journals, owned by Northcliffe Newspapers Group Ltd. The OFT found that Aberdeen Journals was dominant in the market for the supply of advertising space in local newspapers (paid-for and free) within the Aberdeen area. The OFT also concluded that Aberdeen Journals had engaged in predation against its only rival in the relevant market, the *Aberdeen & District Independent*: it deliberately incurred losses on its free newspaper, the Herald & Post, by pricing advertising space at below average variable cost in an attempt to exclude the *Aberdeen & District Independent*. According to the OFT, predatory pricing started in response to the launch of the *Aberdeen & District Independent* in 1996 and continued until 29 March 2000, four weeks after the Competition Act came into force.

In order to assess predation, the OFT conducted an empirical analysis aimed at establishing whether advertising revenues were higher than average variable costs.²⁵ While the Herald & Post did not incur

²⁴The OFT decision of 16 July 2001 was appealed to the Competition Commission Appeal Tribunal (CCAT), which set it aside on the basis that the market definition on which the decision had been made was inadequate. The OFT issued a new decision on 29 September 2002 confirming the original findings. The decision covers a period of infringement from the introduction of the Competition Act on 1 March 2000, which makes the abuse of a dominant position illegal, to 29 March 2000.

²⁵Internal memoranda also showed that the conduct was intentional and that the Herald & Post was subsidized by its parent company Northcliffe Newspapers Group Ltd in order to drive the *Aberdeen & District Independent* out of the market

losses prior to the entry of the Independent, it started to make losses in March 1996 after it heavily decreased advertising rates, increased pagination and increased circulation. The average advertising rate was cut drastically shortly after the launch of the Aberdeen & District Independent in April 2006. It was significantly cut again in October 1998 and the price remained below that level until July 1999. A significant rise took place only in April 2000. Also, the pagination, i.e. the number of pages per month, of the Herald & Post was significantly increased following the launch of the Independent from under 100 pages per month in the period October 1995 to April 1996 to 148 pages in May 1996 and peaking between September 1998 and October 1999 when it was in the range of 350 to 480 pages a month. Lastly, the distribution of the Herald & Post substantially increased after the entry of the Independent from below 100 000 to as much as 126 000 in 1999.

Importantly, the OFT always took into account the costs necessary to serve the readers even if readers did not pay for the product. The OFT noted that whether costs are fixed or variable depends also on the time frame. In particular, it carried out its analysis with reference to both a smaller time frame (the month) and a larger time frame (the alleged predation period). Clearly, considering a larger time frame implies considering more costs as variable and makes a finding of predation more likely. When taking the larger time horizon, the OFT included among variable costs the costs of printing, distribution, editorial staff (i.e. costs on the readers side) and advertising staff (i.e. costs on the advertising side). It thus estimated that The Herald & Post was selling below average variable costs at least until March 2000 included. Furthermore, treating editorial staff and the advertising team as fixed and the cost of printing and distribution (i.e. only costs on the readers side) as variable, the OFT estimated that the Herald & Post's revenues exceeded variable costs only on five occasions between July 1996 and March 2000.

Without access to the data, which were marked as confidential and thus not reported, we cannot check whether indeed the price charged by Aberdeen Journals was predatory. However, even without access to the data, based on the theoretical results in Section 2, we can claim that the OFT applied the correct two-sided Areeda-Tuner rule when it took into account average variable costs related to both sides of the market. In fact, even if on one-side of the market the platform gives away the product for free, as it is the case with free newspapers, then one still needs to apply the two-sided Areeda-Turner rule given by equation (18). However, since on the readers' side of the market the newspaper was given away for free, equation (18) reduces to $P^A - AVC^A - \frac{Q^R}{Q^A} AVC^R < 0$ when the OFT takes as a reference the larger time frame and to $P^A - \frac{Q^R}{Q^A} AVC^R < 0$ when it chooses the shorter time horizon.²⁶

²⁶This is because, according to the OFT, in the shorter time frame all advertising costs were fixed (as they were mostly related to advertising staff).

In other words, although one side of the market does not pay for the product it receives (e.g. here readers do not pay for a copy of the newspaper), still the average variable costs to serve that side of the market need to be taken into account to assess predation.²⁷ Otherwise, one would run the risk of not sanctioning platforms that charge predatory prices in the logic of [Areeda and Turner \(1975\)](#).

4 Conclusion

In their seminal paper, [Areeda and Turner \(1975\)](#) argued that a price below marginal cost should be considered a sign of predation. Recognizing that marginal cost data were typically unavailable, the authors suggested to presume unlawful a price below average variable cost. This Areeda-Turner rule has become the conceptual reference to assess claims of predation. Different authors have highlighted possible short-comings of the rule, while different jurisdictions have adopted different variants of it. A recent survey on predatory pricing is found in [Elzinga and Mills \(2015\)](#)

In our paper, we abstracted from the debate on the limits and merits of the Areeda-Turner rule. We simply recognise its importance in the assessment of predatory pricing and focus instead on the extension of the rule to two-sided markets.

We first showed that a monopolist's price-cost margins in a two-sided market are interrelated. Furthermore, for a two-sided monopolist, even in the absence of actual or potential competition, it may be profit-maximizing to charge a price below marginal cost on one side of the market. As a result, the Areeda-Turner rule that the price is below average variable cost or marginal cost on one side of the market cannot be considered as a sign of predation in two-sided markets.

We then followed the Areeda-Turner logic to derive a corresponding rule for two-sided markets. We argued that one should apply the rule by taking into account revenues and costs from both sides of the market. Hence, in a two-sided market the rule should be rephrased as requiring that the weighted average of the price-cost margins, with the weight given by the marginal network effect, is below the weighted average of the marginal costs. As in a one-sided market, given the difficulty to measure marginal costs, for most practical purposes, courts should presume unlawful a price level below the average variable cost level. The only partial exception to this rule is the particular case in which one of the two sides of the market is indifferent to the other side. In that case, to assess the predatory nature of prices on the side that exerts no externality on the other, a one-sided Areeda-Turner rule can be applied.

²⁷Recognizing that free newspapers also (bear a cost to) serve readers should imply the definition of a relevant market on the readers' side. Interestingly, as shown in [Filistrucchi et al. \(2014\)](#), competition authorities generally fail to define a second relevant market on the side where the product is given away for free. The OFT in Aberdeen journals is no exception.

As applications, we analysed two alleged cases of predatory behaviour in the market for daily newspapers. The first case, the Times-Independent price war, concerns a two-sided market where customers on both sides pay for the product or service they receive. The Independent claimed that the cover prices of The Times were predatory because they were lower than the average variable cost of a copy of the newspaper. We showed that if one took into account the revenues from advertising, as suggested by a 2-sided Areeda-Turner rule, the prices could not be presumed predatory. The Aberdeen Journals case illustrates instead how one should deal with those two-sided markets in which one side of the market does not pay. In fact the case concerned predation by a free daily newspaper. Correctly, the OFT took into account costs from both sides of the market (in addition to the price of advertising) when calculating profit margins. Overall, the discussion of these cases highlights the importance of using the correct Areeda-Turner rule for two-sided markets rather than the traditional one-sided rule.

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